



K25U 0159

Reg. No. : .....

Name : .....

**Sixth Semester B.Sc. Degree (CBCSS – OBE – Regular/Supplementary/  
Improvement) Examination, April 2025  
(2019 to 2022 Admissions)  
CORE COURSE IN MATHEMATICS  
6B11MAT : Complex Analysis**

Time : 3 Hours

Max. Marks : 48

## PART – A

Answer **any 4** questions. **Each** question carries **1** mark.

1. Define a region in complex plane.
2. Evaluate  $\oint_C e^z dz$  where  $C$  is the unit circle in counter clockwise direction.
3. State ML inequality for a complex function  $f(z)$ .
4. What do you mean by singular point of a complex function ?
5. Define residue of a function  $f(z)$  at a singular point  $z_0$ . (4×1=4)

## PART – B

Answer **any 8** questions. **Each** question carries **2** marks.

6. What do you mean by complex continuous function ? Give an example.
7. Show that  $w = e^z$  is analytic everywhere.
8. Solve the equation  $\cos z = 5$ .
9. Evaluate  $\oint_C \bar{z} dz$  where  $C$  is the unit circle in clockwise direction.

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10. Evaluate  $\oint_C \frac{\cos z}{(z - \pi i)^2} dz$  where  $C$  is the circle  $|z| = 4$  in counter clockwise direction.
11. Explain the idea of convergence of complex sequences. Give an example for a convergent complex sequence.
12. Prove that every absolutely convergent series is convergent.
13. Discuss the convergence of 
$$\sum_{n=0}^{\infty} \frac{(100 + 75i)^n}{n!}.$$
14. Find the radius of convergence of the power series 
$$\sum_{n=0}^{\infty} \frac{(2n)!}{(n!)^2} (z - 3i)^n.$$
15. State Laurent's theorem for a complex function  $f(z)$ .
16. Prove that the zeros of a non-zero analytic function  $f(z)$  are isolated. (8×2=16)

## PART – C

Answer **any 4** questions. **Each** question carries **4** marks.

17. Prove that an analytic function whose absolute value is a constant, is a constant function.
18. Prove that the function  $w = \ln z$  analytic everywhere except at zero and on the negative real axis. Also find its derivative.
19. Evaluate  $\int_C (z - z_0)^m dz$  where  $C$  is a circle with center at  $z_0$  and radius  $r$  in counter clockwise direction.



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20. If  $f(z)$  is analytic in a simply connected domain  $D$ , then prove that the integral of  $f(z)$  is independent of path in  $D$ .
21. Discuss the convergence of geometric series.
22. Find all the power series expansions of  $\frac{1}{1-z}$  with center 0.
23. Integrate  $f(z) = \frac{\sin z}{z^4}$  counter clockwise around the unit circle. (4×4=16)

## PART – D

Answer **any 2** questions. **Each** question carries **6** marks.

24. State and prove the necessary condition for a function  $f(z) = u(x, y) + iv(x, y)$  to be analytic at a point  $z_0$ .
25. State and prove Cauchy's integral formula.
26. Find the Taylor's series for the function  $f(z) = \frac{2z^2 + 9z + 5}{z^3 + z^2 - 8z - 12}$  at the point  $z = 1$ .
27. Find all Taylor and Laurent series of  $f(z) = \frac{-2z + 3}{z^2 - 3z + 2}$  with center 0. (2×6=12)