



8. Write the normal form of the equation $AU_{xx} + 2BU_{xy} + CU_{yy} = F(x, y, U, U_x, U_y)$.
9. Prove that $\mu^2 = 1 + \frac{1}{4}\delta^2$.
10. Express $f(x) = \frac{1}{2}(\pi - x)$ as a Fourier series in the interval $0 \leq x \leq 2\pi$.
11. Determine the value of y when $x = 0.1$ given that $y(0) = 1$, $y' = x^2 + y$, $h = 0.05$.
12. Solve $\frac{dy}{dx} = 1 + xy$ with $y(0) = 0$ up to 3rd approximation by Picard's method of successive approximation.
13. Develop the Fourier series of $f(x) = x^2$ in $-2 \leq x \leq 2$.
14. Given $\frac{dy}{dx} = 1 + y^2$ where $y = 0$. When $x = 0$ find $y(0.2)$.
15. Using the table find f as a polynomial in x ,

x	-1	0	3	6	7
$f(x)$	3	-6	39	822	1611

16. Use Euler method to solve $\frac{dy}{dx} = x + xy + y$, $y(0) = 1$. Compute y at $x = 0.15$ by taking $h = 0.15$.

PART - C

Answer any four questions out of seven questions. Each question carries four marks. (4×4=16)

17. From the Taylor series for $y(x)$ find $y(0.1)$ correct to 4 decimal places if $y(x)$ satisfies $y' = x - y^2$ and $y(0) = 1$.
18. Given the differential equation $\frac{dy}{dx} = \frac{x^2}{1+y^2}$ with initial condition $y = 0$ when $x = 0$. Use Picard's method to obtain y for $x = 0.25, 0.5$ and 1.0 , correct to 3 decimal places.



Reg. No. :

Name :

**Sixth Semester B.Sc. Degree (CBCSS – OBE – Regular/Supplementary/Improvement) Examination, April 2024
(2019 to 2021 Admissions)
CORE COURSE IN MATHEMATICS
6B12 MAT : Numerical Methods, Fourier Series and Partial
Differential Equations**

Time : 3 Hours

Max. Marks : 48

PART - A

Answer any four questions out of five questions. Each question carries one mark. (4×1=4)

- Define an even function and give an example.
- Define Newton's divided difference interpolation polynomial.
- Perform 2 iterations of Picard's method to find an approximation solution of the initial value problem $y' = x + y^2$, $y(0) = 1$.
- Find Half Range cosine series for $f(x) = x^2$ in $0 \leq x \leq \pi$.
- Write Laplacian equation in polar coordinates.

PART - B

Answer any eight questions out of eleven questions. Each question carries two marks. (8×2=16)

- Solve $u_{xy} = -u_x$.
- Find the unique polynomial $p(x)$ of degree 2 or less such that $p(1) = 1$, $p(3) = 27$ and $p(4) = 64$ using Lagrange interpolation formula.

P.T.O.



19. Using Lagrange's interpolation formula, find the form of the function $y(x)$ from the following table :

x	0	1	3	4
y	-12	0	12	24

20. Find the fourier series of the periodic function $f(x) = \left(\frac{\pi-x}{2}\right)^2$ in the interval $(0, 2\pi)$.
21. Find the temperature $u(x, t)$ in a laterally insulated copper bar 80 cm long. If the initial temperature is $100 \sin\left(\frac{\pi x}{80}\right)^\circ\text{C}$ and the ends are kept at 0°C , how long will it take for the maximum temperature in the bar to drop to 50°C ?
Physical data for copper : Density = 8.9 g/cm^3 , Specific heat = $0.092 \text{ cal/g}^\circ\text{C}$, thermal conductivity = 0.95 cal/cm sec .
22. Using Newton's forward difference formula, find the sum $S_n = 1^3 + 2^3 + 3^3 + \dots + n^3$.
23. Values of x (in degrees) and $\sin x$ are given in the following table :

x (in degree)	$\sin x$
15	0.2588190
20	0.3420201
25	0.4226183
30	0.5
35	0.5735764
40	0.6427876

Determine the value of $\sin 38^\circ$.

PART - D

Answer any two questions out of four questions. Each question carries six marks. (2×6=12)

24. Derive D'Alembert solution of wave equation.