

Reg. No. :

Name :

V Semester B.Sc. Degree (CBCSS – Supplementary) Examination, November 2023

(2017 and 2018 Admissions) Core Course in Mathematics

5B07 MAT : DIFFERENTIAL EQUATIONS, LAPLACE TRANSFORMS AND FOURIER SERIES

Time: 3 Hours

Max. Marks: 48

SECTION - A

All the first 4 questions are compulsory. They carry 1 mark each.

- 1. Find the curve through the point (1, 1) in the xy plane having at each of its points the slope $\frac{-y}{y}$.
- 2. Solve y'' 4y' + 4y = 0.
- Find the Laplace transform of cos² ωt.
- 4. Find the smallest period p of $\sin \frac{2\pi x}{k}$. (4×1=4)

Answer any 8 questions from among the questions 5 to 14. These questions carry 2 marks each.

- 5. Solve $2xyy' = y^2 x^2$.
- 6. Show that $ye^{x}dx + (2y + e^{x})dy = 0$, y(0) = -1 is exact and solve it.
- 7. Reduce to first order and solve 2xy" = 3y'.
- 8. Find a real general solution of $x^2y'' 2.5xy' 2y = 0$.
- Find a second order homogeneous linear differential equation for which 1 and e^{-2x} are solutions.
- Find ∠ (sinh t cos t).

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- 11. Find Laplace transform of $f(t) = t \sin \omega t$.
- 12. Let $\mathcal{L}(f) = \frac{1}{s^2(s^2 + \omega^2)}$. Find f(t).
- 13. What are the Euler's formulas?
- 14. What is the Fourier integral representation?

(8×2=16)

SECTION - C

Answer any 4 questions from among the questions 15 to 20. These questions carry 4 marks each.

- 15. Using Picard's iteration, find an approximate solution to the initial value problem $y' = 1 + y^2$, y(0) = 0.
- 16. Solve the boundary value problem y'' + 4y = 0, y(0) = 3, $y(\frac{\pi}{2}) = -3$. 17. Solve the initial value problem y'' + y = 2x, y(0) = -1, y'(0) = 8.
- 18. Using the Laplace transform, solve $y'' + 6y' + 8y = e^{-3t} e^{-5t}$, y(0) = 0, y'(0) = 0.
- 19. Find the Fourier cosine series of the function $f(x) = \pi x$ in $0 < x < \pi$.
- 20. Find the Fourier cosine integral of $f(x) = e^{-kx}$.

 $(4 \times 4 = 16)$

SECTION - D

Answer any 2 questions from among the questions 21 to 24. These questions carry 6 marks each.

- 21. Solve y'' + 3y' + 2y = 0 by converting into a system of two first order differential equations.
- 22. Find the general solution of y'' + 9y = csc3x.
- 23. Solve the initial value problem y'' 3y' + 2y = 4t, y(0) = 1, y'(0) = -1 using Laplace transform.
- 24. Find the Fourier series of the function $f(x) = 1 x^2$, -1 < x < 1, p = 2. (2×6=12)