G CET WALLIGRARY

Reg. No.:....

# VI Semester B.Sc. Degree (CBCSS - Reg./Supple./Improv.) Examination, April 2020 (2014 Admission Onwards) **CORE COURSE IN MATHEMATICS** 6B14MAT (Elective A): Operations Research

Time: 3 Hours

#### SECTION - A

All the first 4 questions are compulsory. They carry 1 mark each.

- 1. Define global minimum of a function f(x).
- 2. What do you mean by degeneracy in a linear programming problem ?
- 3. What is assignment problem?
- 4. Define saddle point of a game.

#### SECTION - B

Answer any 8 questions from among the questions 5 to 14. These questions carry 2 marks each.

- 5. Show that the function  $f((x_1,x_2))=x_1^2+x_2^2$  is a convex function over all of  $R^2$ .
- 6. Determine whether the quadratic form  $2x_1^2 + 6x_2^2 6x_1x_2$  is positive definite or negative definite.
- 7. Define the term basic solution. How many basic solutions are there to a given system of two simultaneous linear equation in four unknowns?
- 8. State the general LPP in the canonical form.
- 9. Explain least cost method to solve transportation problem for an initial solution.

P.T.O.

- 10. What is degeneracy in transportation problems?
- 11. Give two applications of assignment problem.
- 12. Define the sequencing problem with n jobs and two machines.
- 13. What assumptions are made in the theory of games?
- 14. Explain the dominance property in game theory.

### SECTION - C

Answer any 4 questions from among the questions 15 to 20. These questions carry 4 marks each.

- 15. Let f(x) be a convex function on a convex set S. Prove that f(x) has a local minimum on S, then this local minimum is also a global minimum on S.
- 16. Solve graphically Max  $Z = 80x_1 + 55x_2$

Subject to 
$$4x_1 + 2x_2 \le 40$$

$$2x_1 + 4x_2 \le 32 \ x_1 \ge 0, x_2 \ge 0.$$

17. Obtain an initial basic feasible solution to the following transportation problem:

	D	E	F	G	available
Α	11	13	17	14	250
В	16	18	14	10	300
С	21	24	13	10	400
requirement	200	225	275	250	

- 18. Show that the optimal solution of a assignment problem is unchanged if we add or subtract the same constant to the entries of any row or column of the cost matrix.
- 19. Explain the sequencing problem with n jobs and k machines.
- 20. Explain the graphical method of solving a game.

## SECTION - D

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Answer any 2 questions from among the questions 21 to 24. These questions carry 6 marks each.

- 21. Define the dual of a linear programming problem. Prove that the dual of the dual is the primal.
- 22. Solve the following transportation problem.

	Х	Υ	Z	Availability
A	50	30	220	1
В	90	45	170	3
C	250	200	50	4
requirement	4	2	2	

- 23. Explain the Hungarian method to solve an assignment problem.
- 24. Describe the procedure to solve any 2×2 two person zero sum game without any saddle point.

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