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Reg. No. :

Name :

I Semester B.Sc. Degree (C.B.C.S.S. – Reg./Supple./Improv.)

Examination, November 2017

CORE COURSE IN MATHEMATICS

1B01 MAT : Differential Calculus (2014 – 16 Admns.)

Time: 3 Hours Max. Marks: 48

SECTION-A

All the first 4 questions are compulsory. They carry 1 mark each.

- 1. Evaluate $\lim_{x\to 1} \frac{x^2+x-2}{x^2-x}$.
- 2. For what value of a is $f(x) = \begin{cases} x^2 1 & x < 3 \\ 2ax & x \ge 3 \end{cases}$ is continuous at every x?
- 3. Evaluate $\lim_{x\to 0} \frac{1-\cos x}{x+x^2}$.
- 4. State Rolle's theorem.

 $(1 \times 4 = 4)$

SECTION-B

Answer any 8 questions from among the questions 5 to 14. These questions carry 2 marks each.

- 5. Given f(x) = 5 4x, find $f^{-1}(x)$ and evaluate df^{-1}/dx at x = f(1/2).
- Find the equation of the sphere which has its centre at the origin and which passes through the point (2, 3, 6).
- 7. Find $\lim_{x\to\infty} x^{1/x}$.

P.T.O.



- 8. Obtain the Maclaurin series for esin x upto the term containing x2.
- 9. Find the radius of curvature at any point of the curve : x = 2t, $y = t^2 1$.
- 10. Find the asymptotes of the curve $x^2y^2 x^2y xy^2 + x + y + 1 = 0$.
- 11. Show that $f(x, y) = \begin{cases} \frac{2xy}{x^2 + y^2}, & \text{if } (x, y) \neq (0, 0) \\ 0, & \text{if } (x, y) = (0, 0) \end{cases}$ is discontinuous at the origin.
- 12. Find the values of $\frac{\partial f}{\partial x}$ and $\frac{\partial f}{\partial y}$ at point (4, -5) if $f(x, y) = x^2 + 3xy + y 1$.
- 13. Find the linearization of $f(x, y) = x^2 xy + \frac{1}{2}y^2 + 3$ at the point (3, 2).
- 14. If $u = ze^{ax+by}$, where z is a homogeneous function in x and y of degree n, prove

that
$$x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = (ax + by + n)u$$
. (2x8=16)

SECTION-C

Answer any 4 questions from among the questions 15 to 20. These questions carry 4 marks each.

- 15.a) Find the derivative of $y = \cos^{-1} x x \sec h^{-1} x$ with respect to x.
 - b) Find $\lim_{x\to 0} x^2 e^{\sin x}$
- 16. Find the nth derivative of cos x cos 2x cos 3x.
- 17. In spherical polar coordinates, a certain surface is described by the equation $\rho = 2\cos\phi$. Find its equation in Cartesian coordinates and cylindrical coordinates.



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- 18. Find the inflection point of the curve $y = \frac{x^3}{3} \frac{x^2}{2} 2x + \frac{1}{3}$. Identify the intervals on which it is concave up and concave down.
- 19. For $g(x) = \frac{x-4}{x-3}$, decide if we can use Lagrange's mean value theorem on [4, 6]. If so, find c. If not, explain why.
- 20. Find $\frac{\partial w}{\partial r}$ and $\frac{\partial w}{\partial s}$ in terms of r and s if $w = x + 2y + z^2$, $x = \frac{r}{s}$, $y = r^2 + \ln s$, z = 2r. (4x4=16)

SECTION-D

Answer any 2 questions from among the questions 21 to 24. These questions carry 6 marks each.

- 21. If $y = e^{a\sin^{-1}x}$, prove that $(1 x^2)y_{n+2} (2n + 1)xy_{n+1} (n^2 + a^2)y_n = 0$. Hence find the value of y_n when x = 0.
- 22. Find the equation of the right circular cone whose vertex is at the origin and which passes through the straight lines

$$\frac{x}{3} = \frac{y}{6} = \frac{z}{-2};$$
 $\frac{x}{2} = \frac{y}{2} = \frac{z}{-1};$ $\frac{x}{-1} = \frac{y}{2} = \frac{z}{2}.$

Find the axis and the semivertical angle of the cone.

- 23. Show that the right circular cylinder of given surface (including the ends) and maximum volume is such that its height is equal to the diameter of the base.
- 24. If V = log_e sin $\left[\frac{\pi(2x^2 + y^2 + xz)^{1/2}}{2(x^2 + xy + 2yz + z^2)^{1/3}}\right]$, find the value of $x\frac{\partial V}{\partial x} + y\frac{\partial V}{\partial y} + z\frac{\partial V}{\partial z}$ when x = 0, y = 1, z = 2. (6x2=12)