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29. Two sets of 100 students each were taught to read by two different methods. After the instructions were over,a reading test given to them revealed.

(4)

	Method 1	Method 2
Mean score	73.4	70.3
SD	8	10

30. During a country wide investigation, the incidence of T.B was found to be 1%. In a state, out of 400 sample, 5 were affected, whereas in another state 10 out of 1200 sample were affected. Does this indicate any significant difference. 

K19U 3018

Name : .....

Reg. No.:....

III Semester B.Sc.Hon's (Mathematics) Degree (Reg./Supple./ Improv.)
Examination, November 2019

(2016 ADMISSION ONWARDS)

## BHM 304: THEORY OF SAMPLING AND ESTIMATION

Time: 3 Hours

Max. Marks: 60

## **SECTION - A**

Answer any 4 questions out of 5.

 $(4 \times 1 = 4)$ 

- 1. Define Standard error. What is the standard error of the mean of a sample of size n taken from a population with  $SD^{\sigma}$ ?
- 2. Define unbiased estimator. Give an unbiased estimator of the mean of a population.
- 3. What are the properties of MLE?
- 4. Define critical region.
- 5. Define power of a test.

#### **SECTION - B**

Answer any 6 questions out of 9.

 $(6 \times 2 = 12)$ 

- 6. Distinguish between parameter and statistic.
- 7. Define consistency of an estimator.
- 8. State Central limit theorem.
- A sample of size 400 is taken from a population where standard deviation is 16. Find the values of standard error and probable error.
- 10. Distinguish between point estimators and interval estimators.
- 11. If t is an unbiased estimator of the parameter  $\theta$ , show that t² is a biased estimator of  $\theta^2$ .

P.T.O.

- 12. A random sample of 50 items drawn from a particular population has a mean 30 with a standard deviation 28. Construct 98% confidence interval estimate of the population mean.
- 13. If x has the binomial distribution with parameters n and p, show that the sample proportion,  $\frac{x}{n}$  is an unbiased estimator of p.
- Distinguish between one tailed and two tailed tests. Give one example for each.

## SECTION - C

Answer any 8 questions out of 12.

 $(8 \times 4 = 32)$ 

- 15. A cubical die was thrown 9000 times and a 2 or 3 were obtained 3286 times. On the assumption of random trials, do the data indicate an unbiased one.
- 16. A sample of 900 days is taken from the meteorological records of a certain district and 100 of them are found to be foggy. What are the probable limits to the percentage of foggy days in the district.
- 17. If  $x_1, x_2, \dots, x_n$  be a random sample of size n from a normal distribution, with mean zero and variance  $\sigma^2$ . Show that  $\sum_{r=1}^n \frac{{x_1}^2}{n}$  is an unbiased estimator of  $\sigma^2$
- 18. Write the confidence intervals of the mean when
  - i) The population standard deviation is known
  - ii) The population standard deviation is unknown.
- 19. Describe Bayesian estimation.
- 20. In a random selection of 50 of 600 road crossings in a town, the mean number of automobile accidents per year was found to be 3.8 and the sample standard deviation was 0.8. Construct a 90% confidence interval for the mean number of automobile accidents per crossing per year.



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- 21. A random sample of size 20 is taken from a normal population with variance 225 has sample mean 64.3. Find the confidence interval for the mean.
- 22. The average marks in mathematics of a sample of 100 students was 51 with a standard deviation of 6 marks. Could this have been a random sample from a population with average marks of 50.
- 23. Random samples drawn from two places gave the following data relating to the heights of children.

	Place A	Place B
Mean height	68.5	68.58
SD	2.5	3.0
Sample size	1200	1500

Test at 5% level that the mean height is the same for the children at two places.

# 24. Explain

- Simple random sampling
- ii) Stratified sampling.
- 25. A machine puts out 16 imperfect articles in a sample of 500. After the machine is overhauled, it puts out 3 imperfect articles in a batch of 100. Has the machine improved.
- 26. In a random sample of 125 people, 68 people consumes soft drinks. Test the hypothesis that the proportion of people consumes soft drink is 0.5.

#### SECTION - D

Answer any 2 questions out of 4.

 $(2 \times 6 = 12)$ 

- 27. A random sample of size 100 is taken from an infinite population having the mean  $\mu$ =76 and the variance =256. What is the probability that the sample mean  $\bar{\chi}$  will be between 75 and 78.
- **28.** Obtain an unbiased estimator of  $\theta = \sigma^2$  for a normal distribution with mean  $\mu$  and variance  $\sigma^2$ . for a normal distribution with mean  $\mu$  and variance  $\sigma^2$ .

P.T.O.